

Physics 104

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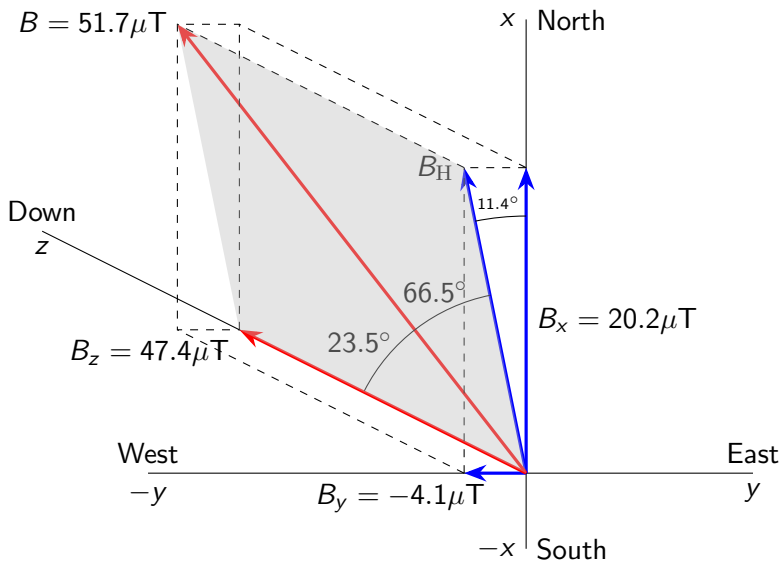
Earth's magnetic field in Annville, PA

B_x	$20.2 \mu\text{T}$	x is North
B_y	$-4.1 \mu\text{T}$	y is East
B_z	$47.4 \mu\text{T}$	z is Down
Horizontal Intensity	$20.6 \mu\text{T}$	
Total Field	$51.7 \mu\text{T}$	
Inclination (+ D , - U)	66.5°	
Declination (+ E , - W)	-11.4°	

Data source:

<https://www.ngdc.noaa.gov/geomag/calculators/magcalc.shtml#igrfmm>

Earth's magnetic field in Annville, PA



Lenz's law

External magnetic flux	Induced magnetic flux	Induced emf
out of board, increasing	into board	clockwise
out of board, decreasing	out of board	counter-clockwise
into board, increasing	out of board	counter-clockwise
into board, decreasing	into board	clockwise

Theories in Physics

nonrelativistic quantum

wave
mechanics
Schrödinger
1926

electricity
Coulomb
1800

wave optics
Young
1803

mechanics
Newton
1687

gravity
Newton
1687

nonrelativistic classical

relativistic quantum

QED
Feynman
1949

Electroweak
Weinberg
1967

QCD
Wilczek
1973

quantum
gravity
?

EM Theory
Maxwell
1865

SR
Einstein
1905

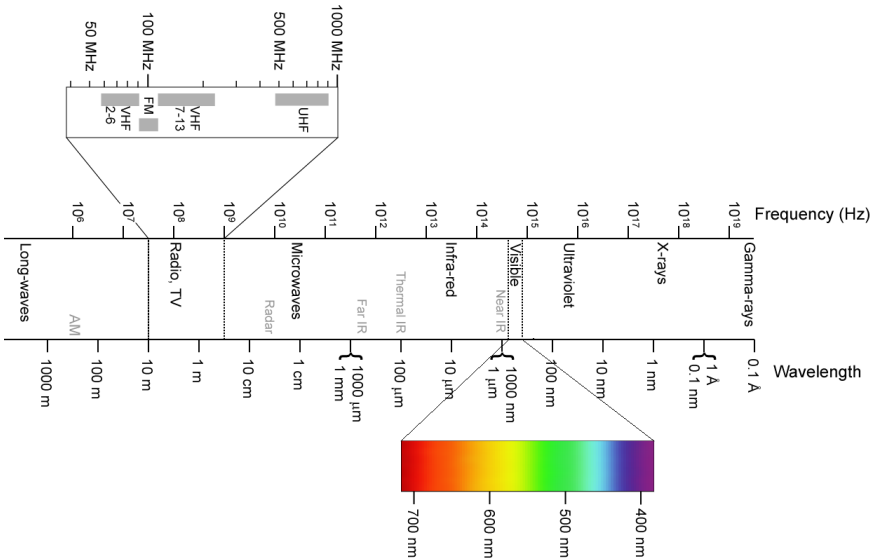
GR
Einstein
1915

relativistic classical

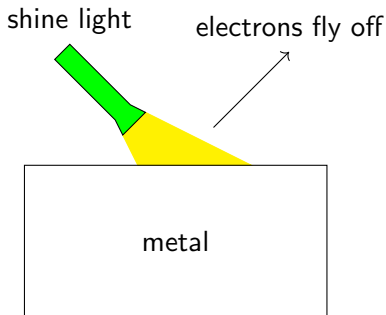
Four theories of light

- ▶ Light is a ray
 - ▶ Geometrical Optics
- ▶ Light is a wave (Young, 1803)
 - ▶ Wave Optics
- ▶ Light is an electromagnetic wave (Maxwell, 1865)
 - ▶ Classical Electromagnetic Theory (EM Theory)
- ▶ Light is a quantum field
 - ▶ Photon Theory (starting with Planck and Einstein, 1900–1905)
 - ▶ QED (Quantum Electrodynamics, 1949)

The electromagnetic spectrum

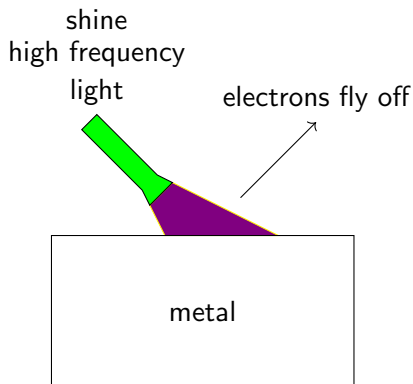


The photoelectric effect

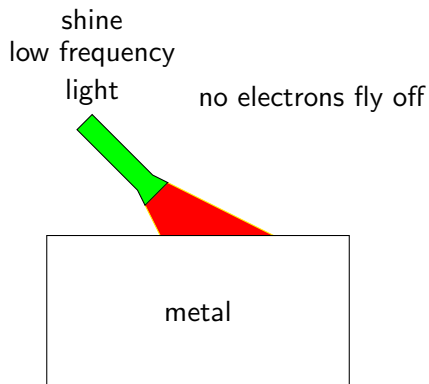


- ▶ Light provides the energy needed to free electrons from the metal.

The photoelectric effect



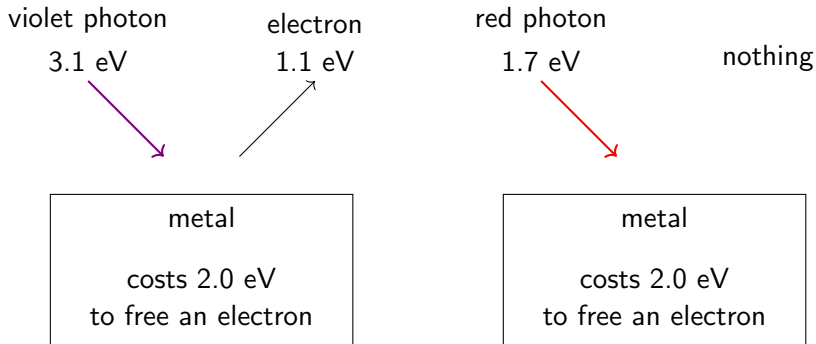
- ▶ violet has high frequency



- ▶ even if light is very bright

The photoelectric effect: Einstein's idea

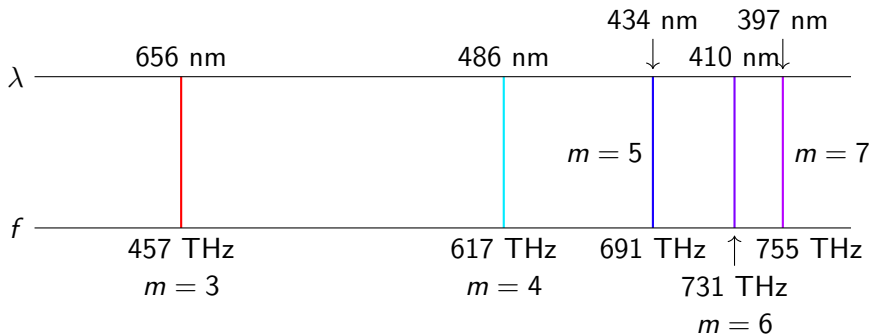
- ▶ One photon must free one electron.
- ▶ Energy of one photon is $E = hf$.



Key events in the development of Quantum Theory

- 1900 Planck proposes quanta of light
- 1905 Einstein explains photoelectric effect
- 1913 Bohr suggests special radii
- 1921 Stern and Gerlach demonstrate spatial quantization
- 1923 Compton sees frequency shift in scattered X-rays
- 1924 de Broglie suggests matter waves
- 1925 Heisenberg presents matrix mechanics
- 1926 Schrödinger presents wave mechanics
- 1927 Heisenberg presents uncertainty principle

Balmer (1885) looked at 5 lines from hydrogen



He found a pattern:

$$\lambda = \frac{365 \text{ nm}}{1 - \frac{4}{m^2}}$$

$$f = 3289 \text{ THz} \left(\frac{1}{2^2} - \frac{1}{m^2} \right)$$

Circumference as a function of velocity

As a model for hydrogen, suppose electron is in uniform circular motion around proton because of Coulomb's law:

$$k \frac{|q_e q_p|}{r^2} = m_e \frac{v^2}{r}$$

Solve for r :

$$r = \frac{k |q_e q_p|}{m_e v^2}$$

Circumference is $2\pi r$:

$$C = \frac{2\pi k |q_e q_p|}{m_e v^2}$$

Wavelength as a function of velocity

In preparation for Bohr's idea, we use the quantum idea of how momentum is related to wavelength

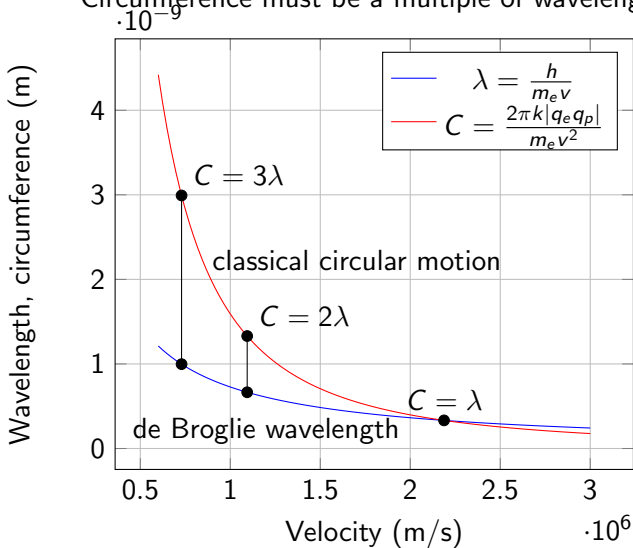
$$p = \frac{h}{\lambda}$$

to get an expression for wavelength as a function of velocity. Solve this equation for wavelength and use $m_e v$ for the momentum of the electron.

$$\lambda = \frac{h}{p} = \frac{h}{m_e v}$$

Bohr atom (1913)

Circumference must be a multiple of wavelength



Energy of electron in hydrogen

Electron energy consists of kinetic energy and potential energy:

$$E = \frac{1}{2}m_e v^2 + k \frac{q_e q_p}{r}$$

Uniform circular motion equation

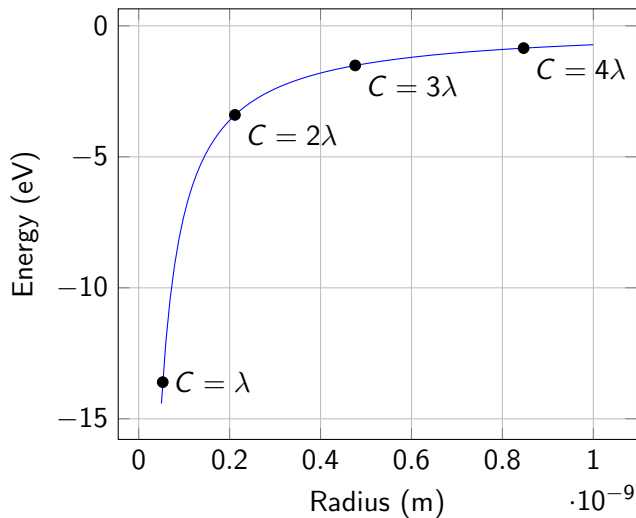
$$k \frac{|q_e q_p|}{r^2} = m_e \frac{v^2}{r}$$

allows us to solve for v in term of r so that we can write E in terms of r .

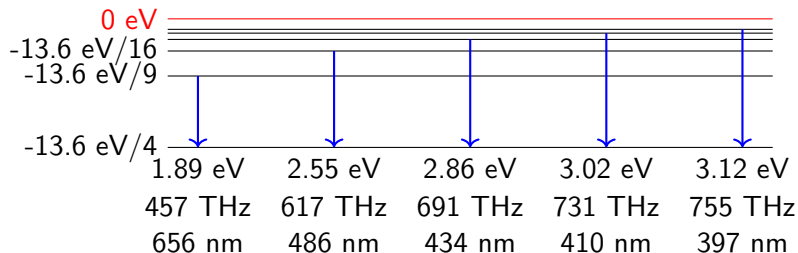
$$E = \frac{1}{2}k \frac{|q_e q_p|}{r} + k \frac{q_e q_p}{r} = -\frac{1}{2}k \frac{|q_e q_p|}{r}$$

Bohr model produces hydrogen energy levels

Only certain radii are allowed



Hydrogen energy levels



Differences in energy levels
match the Balmer frequencies

-13.6 eV